Word Problem

Review

1. Jason jumped off of a cliff into the ocean in Acapulco while vacationing with some friends. His height as a function of time could be modeled by the function $h(t) = -16t^2 + 16t + 480$, where t is the time in seconds and h is the height in feet.

   a. How long did it take for Jason to reach his maximum height?

   b. What was the highest point that Jason reached?

   c. ~~Jason hit the water after how many seconds?~~

$$h(t) = -16t^2 + 16t + 480$$

(a) find x-value of vertex

$$x = \frac{-b}{2a}$$

$$x = \frac{-(16)}{2(-16)} = \frac{1}{2}$$

$$\boxed{\frac{1}{2} \text{ second}}$$

(b) find y-value of vertex

$$y = -16\left(\frac{1}{2}\right)^2 + 16\left(\frac{1}{2}\right) + 480$$

$$y = -4 + 8 + 480$$

$$y = 484$$

$$\boxed{484 \text{ ft}}$$

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2. If a toy rocket is launched vertically upward from ground level with an initial velocity of 128 feet per second, then its height h after t seconds is given by the equation $h(t) = -16t^2 + 128t$ (if air resistance is neglected).

a. How long will it take for the rocket to return to the ground?

b. After how many seconds will the rocket be 112 feet above the ground?

c. How long will it take the rocket to hit its maximum height?

d. What is the maximum height?

$h(t) = -16t^2 + 128t$

© Find x-value of vertex

$x = \dfrac{-b}{2a}$

$x = \dfrac{-128}{2(-16)} = 4$

4 seconds

ⓓ Find y-value of vertex

$y = -16(4)^2 + 128(4)$

$y = -256 + 512$

256 ft

$y = 256$

4. You and a friend are hiking in the mountains. You want to climb to a ledge that is 20 ft. above you. The height of the grappling hook you throw is given by the function $h(t) = -16t^2 - 32t + 5$. What is the maximum height of the grappling hook? Can you throw it high enough to reach the ledge?

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$$n(t) = -16t^2 - 32t + 5$$

Max height = y value of vertex

$$x = \frac{-(-32)}{2(-16)} = -1$$

$$y = -16(-1)^2 - 32(-1) + 5$$
$$y = -16 + 32 + 5$$
$$y = 21 \qquad \boxed{21 \ ft}$$

$$\boxed{21 \ ft > 20 \ ft \qquad yes, \ you \ can \ throw \ it \ high \ enough}$$

5. You are trying to dunk a basketball. You need to jump 2.5 ft. in the air to dunk the ball. The height that your feet are above the ground is given by the function $h(t) = -16t^2 + 12t$. What is the maximum height your feet will be above the ground? Will you be able to dunk the basketball?

$$h(t) = -16t^2 + 12t$$

max height = y-value of vertex

$$x = \frac{-b}{2a} \qquad x = \frac{-(12)}{2(-16)} = \frac{12}{32} = \frac{3}{8}$$

$$y = -16\left(\frac{3}{8}\right)^2 + 12\left(\frac{3}{8}\right) \qquad \frac{18}{4} - \frac{9}{4} = \frac{9}{4}$$

$$y = -\frac{9}{4} + \frac{9}{2}$$

$$y = \frac{9}{4} = \boxed{2.25 \text{ ft}}$$

$$2.25 < 2.5 \qquad \boxed{\text{no you cannot dunk}}$$